B. Find these Vector Components and write each vector as a proper component vector:



### 3.1 Vector Quizlette

C. Add these component vectors:

D. Draw these vectors as Angle Magnitude vectors. The vector should be an arrow, and calculate and label its magnitude (hypotenuse) and the angle:

1) $6.00 \mathrm{mx}+8.00 \mathrm{my}$
2) $-4.50 \mathrm{mx}+6.40 \mathrm{my}$
3) $-5.12 \mathrm{mx}+-3.90 \mathrm{my}$
4) $56.3 \mathrm{mx}+-37.0 \mathrm{my}$

### 3.1 Vector Quizlette

E1: Adding two Angle Magnitude Vectors (Just like the test...)

Find the Components of these two vectors:
Carry three decimal places in your calculations.

Mag. $=12.0 \mathrm{~m}, \quad \theta=21.0^{\circ}$


$$
1=\ldots x+\ldots y
$$

Mag. $=8.00 \mathrm{~m}, \theta=17.0^{\circ}$


$$
2=
$$

$\qquad$ X + $\qquad$

Add the Two Vectors: $1+2=$ $\qquad$ X + $\qquad$

Draw a picture of the resultant vector with its tail on the origin, find its magnitude, and label an angle indicating its direction:

14.9 m , up and right, above $53.4^{\circ}$ the x -axis

### 3.1 Vector Quizlette

E2: Adding two Angle Magnitude Vectors
Find the Components of these two vectors:
Carry three decimal places in your calculations.

$$
2=
$$

$\qquad$ X + $\qquad$

Mag. $=42.0 \mathrm{~m}, \theta=12^{\circ}$

Add the Two Vectors: $1+2=$ $\qquad$ x + $\qquad$

Draw a picture of the resultant vector with its tail on the origin, find its magnitude, and label an angle indicating its direction:


34.9 m , right and down at $37^{\circ}$ below the x axis

Name
Carry three decimal places in your calculations.
When you have finished this, go to the website and check your answers. If you got a problem wrong, cross it off on the front, and do it correctly on the back. Find the Components of these two vectors:


$$
\text { Mag. }=13.4 \mathrm{~m}, \theta=42.0^{\circ}
$$

$$
1=\ldots \quad \mathrm{x}+\ldots
$$

$2=$ $\qquad$ $\mathrm{x}+$ $\qquad$


Mag. $=6.12 \mathrm{~m}, \theta=11.3^{\circ}$

Add the Two Vectors: $1+2=$ $\qquad$ x + $\qquad$

Draw a picture of the resultant vector with its tail on the origin, find its magnitude, and label an angle indicating its direction:

### 3.2 Cliff Problem Quizlette (turn this in)

Name

1. Red Elk runs at a speed of $9.20 \mathrm{~m} / \mathrm{s}$ horizontally off a cliff that is $\mathbf{6 . 4 0} \mathbf{~ m}$ above the water.
A) Set up your horizontal/vertical table, fill it with known quantities, and solve for everything you don't know. (You know horizontally: both velocities and the acceleration, and vertically: the displacement, the initial velocity, and the acceleration)


| B) What time is he in the air? <br> $(1.14 \mathrm{~s})$ | C) What is his final vertical <br> velocity of impact? (Just before <br> he hits the water) <br> $(-11.2 \mathrm{~m} / \mathrm{s})$ | D) How far from the base of the <br> cliff does he hit the water? <br> $(10.5 \mathrm{~m})$ |
| :--- | :--- | :--- |
| E) Draw a picture of his final velocity of impact. Calculate the <br> speed he is traveling, and find the angle below horizontal his <br> velocity makes. $\left(14.5 \mathrm{~m} / \mathrm{s}, 50.6^{\circ}\right.$ below horiz. $)$ | F) What is his speed of impact <br> with the water? $(14.5 \mathrm{~m} / \mathrm{s})$ |  |

2. Red Elk runs with a purely horizontal velocity and lands 8.50 m from the base of the cliff 1.20 seconds later.

| a. How high is the cliff? | b. What was his horizontal <br> velocity? | c. What is his final vertical <br> velocity? |
| :--- | :--- | :--- |

d. Draw a picture of his final velocity of impact. Calculate the speed he is traveling, and find the angle below horizontal his velocity makes.

3. Red Elk runs with a purely horizontal velocity of $5.60 \mathrm{~m} / \mathrm{s}$ and hits the water 1.80 seconds later.

| a. How high is the cliff? | b. How far from the base of the <br> cliff does he land? | c. What is his final vertical <br> velocity? |
| :--- | :--- | :--- |

d. Draw a picture of his final velocity of impact. Calculate the speed he is traveling, and find the angle below horizontal his velocity makes.


| a. What time was he in the air? | b. How high is the cliff? | c. What is his final vertical <br> velocity? |
| :--- | :--- | :--- |

d. Draw a picture of his final velocity of impact. Calculate the speed he is traveling, and find the angle below horizontal his velocity makes.

5. Red Elk runs with a purely horizontal velocity and lands 8.60 m from the base of a 13.0 m tall cliff.

| a. What time is he in the air? | b. What is his horizontal <br> velocity? | c. What is his final vertical <br> velocity? |
| :--- | :--- | :--- |

d. Draw a picture of his final velocity of impact. Calculate the speed he is traveling, and find the angle below horizontal his velocity makes.
a) 1.629 s, b) $5.280 \mathrm{~m} / \mathrm{s}$, c) $-15.962 \mathrm{~m} / \mathrm{s}$, d) $16.8 \mathrm{~m} / \mathrm{s}$ at $71.7^{\circ}$ below horiz.

## FA 3.2 - Cliff Problems

Name
Show your work and circle your answers to receive full credit. Ignore air friction, use the convention that down is negative, and use $g=9.80 \mathrm{~m} / \mathrm{s} / \mathrm{s}$.
When you have finished this, go to the website and check your answers. If you got a problem wrong, cross it off on the front, and do it correctly on the back.
A ball rolls off the edge of a 15.0 m tall cliff with a purely horizontal velocity, and strikes the ground at a distance of $\mathbf{1 2 . 4} \mathbf{~ m}$ from the base of the cliff.

1. What time was the ball in the air?
2. What was the ball's horizontal velocity?
3. What is the final vertical velocity? (Just before it hits the ground)

4-5: Draw a picture of the final velocity of impact. Calculate the speed it is traveling, and find the angle below horizontal the velocity makes.

## P3.2 Cliff Practice Problems (Optional)

Round to three figures, Ignore air friction and use the convention that down is negative. $g=9.80 \mathrm{~m} / \mathrm{s} / \mathrm{s}$

| $\begin{aligned} & 1.25 \mathrm{~s} \\ & 9.07 \mathrm{~m} / \mathrm{s} \\ & -12.2 \mathrm{~m} / \mathrm{s} \\ & 15.2 \mathrm{~m} / \mathrm{s}, 53.4^{\circ} \mathrm{blw} \mathrm{hrz} \end{aligned}$ | 1. A ball is projected with a purely horizontal velocity from an 7.60 m tall cliff and lands 11.3 m from the base of the cliff. <br> a. What time is the ball in the air? <br> b. With what purely horizontal velocity was it projected from the top of the cliff? <br> c. What is the final vertical velocity? (Just before it hits the ground) <br> d. Draw a picture of the final velocity of impact. Calculate the speed it is traveling, and find the angle below horizontal the velocity makes. |
| :---: | :---: |
| $\begin{aligned} & 19.6 \mathrm{~m} \\ & 2.00 \mathrm{~s} \\ & -19.6 \mathrm{~m} / \mathrm{s} \\ & 23.2 \mathrm{~m} / \mathrm{s}, 57.5^{\circ} \mathrm{blw} \mathrm{hrz} \end{aligned}$ | 2. A ball leaves the edge of a cliff with a purely horizontal velocity of $12.5 \mathrm{~m} / \mathrm{s}$, and lands 25.0 m from the base of the cliff <br> a. How high is the cliff? <br> b. What time does it take the ball to hit the ground? <br> c. What is the final vertical velocity? (Just before it hits the ground) <br> d. Draw a picture of the final velocity of impact. Calculate the speed it is traveling, and find the angle below horizontal the velocity makes. |
| $\begin{aligned} & 9.88 \mathrm{~m} \text { high } \\ & 12.9 \mathrm{~m} \\ & -13.9 \mathrm{~m} / \mathrm{s} \\ & 16.6 \mathrm{~m} / \mathrm{s}, 56.8^{\circ} \mathrm{blw} \mathrm{hrz} \end{aligned}$ | 3. A ball rolls off the edge of a cliff. The instant it leaves the edge, it has a purely horizontal velocity of $9.10 \mathrm{~m} / \mathrm{s}$, and it strikes the ground after 1.42 seconds. <br> a. How high is the cliff? <br> b. How far from the base of the cliff does the ball land? <br> c. What is the final vertical velocity? (Just before it hits the ground) <br> d. Draw a picture of the final velocity of impact. Calculate the speed it is traveling, and find the angle below horizontal the velocity makes. |
| $\begin{aligned} & 1.41 \mathrm{~s} \\ & 19.0 \mathrm{~m} \\ & -13.8 \mathrm{~m} / \mathrm{s} \\ & 19.3 \mathrm{~m} / \mathrm{s}, 45.6^{\circ} \mathrm{blw} \mathrm{hrz} \end{aligned}$ | 4. A ball is projected sideways at $13.5 \mathrm{~m} / \mathrm{s}$ from the top of a 9.70 m tall cliff. <br> a. What time is the ball in the air? <br> b. How far from the base of the cliff does the ball land? <br> c. What is the final vertical velocity? (Just before it hits the ground) <br> d. Draw a picture of the final velocity of impact. Calculate the speed it is traveling, and find the angle below horizontal the velocity makes. |
| $\begin{aligned} & 20.6 \mathrm{~m} \text { high } \\ & 10.5 \mathrm{~m} / \mathrm{s} \\ & -20.1 \mathrm{~m} / \mathrm{s} \\ & 22.7 \mathrm{~m} / \mathrm{s}, 62.3^{\circ} \mathrm{blw} \mathrm{hrz} \end{aligned}$ | 5. A ball rolls off the edge of a cliff with a purely horizontal velocity, and strikes the ground 2.05 s later at a distance of 21.6 m from the base of the cliff. <br> a. How high is the cliff? <br> b. What was the ball's horizontal velocity? <br> c. What is the final vertical velocity? (Just before it hits the ground) <br> d. Draw a picture of the final velocity of impact. Calculate the speed it is traveling, and find the angle below horizontal the velocity makes. |

Red Elk shoots an air rocket at a speed of $25.0 \mathrm{~m} / \mathrm{s}$ at an angle of $57.0^{\circ}$ above the horizontal on a very level field.
A) Break the velocity vector into components. (These become your initial velocities for x and y ) Set up your horizontal/vertical table, fill it with known quantities, and solve for everything you don't know. (You know horizontally: both velocities and the acceleration, and vertically: the displacement, both velocities, and the acceleration) $(13.616 \mathrm{~m} / \mathrm{s} x+20.967 \mathrm{~m} / \mathrm{s}$ y)


| B) What are the initial horizontal <br> and vertical velocity <br> components? ${ }_{(13.616 \mathrm{~m} / \mathrm{sx}+20.967 \mathrm{~m} / \mathrm{s})}$ | C) What time is the rocket in the <br> air? ${ }_{(4.27 \mathrm{~s})}$ | D) How far does the rocket go <br> before hitting the ground? ${ }_{(5.2 \mathrm{~m})}$ |
| :--- | :--- | :--- |
| E) What is the greatest height the rocket reaches? $(22.4 \mathrm{~m})$ | F) What is the speed of the <br> rocket at the highest point? <br> $(13.6 \mathrm{~m} / \mathrm{s})$ |  |

Red Elk kicks a ball at a speed of $28.0 \mathrm{~m} / \mathrm{s}$ at an angle of $34.0^{\circ}$ above the horizontal on a very level field.

1. What time is the ball in the air? ${ }_{(3.20 \mathrm{~s})}$
2. What horizontal distance does it travel before hitting the ground again? (74.2 m)
3. What is the greatest height the ball reaches? What is its speed at this height? ( $12.5 \mathrm{~m}, 23.2 \mathrm{~m} / \mathrm{s}$ )

Use the range equation to find these ranges for the velocities and launch angles. Write down what you put into your calculator:

Velocity $=32.0 \mathrm{~m} / \mathrm{s}$, Launch Angle $=47.0^{\circ}$ Range $=$ $\qquad$ ( 104 m )

Velocity $=11.0 \mathrm{~m} / \mathrm{s}$, Launch Angle $=26.0^{\circ}$ Range $=$ $\qquad$ ( 9.73 m )

Use the range equation to find the proper launch angles for the following velocities and ranges. Write down what you put into your calculator:

Velocity $=29.0 \mathrm{~m} / \mathrm{s}$, Range $=32.0 \mathrm{~m}$, Launch Angles $=$ $\qquad$ and $\qquad$ degrees (10.9 $9^{\circ}$ and $79.1^{\circ}$ )

Velocity $=12.0 \mathrm{~m} / \mathrm{s}$, Range $=14.5 \mathrm{~m}$, Launch Angles $=$ $\qquad$ and $\qquad$ degrees

Name $\qquad$
Show your work and circle your answers to receive full credit (but don't round until the end) Ignore air friction, use the convention that down is negative, and use $g=9.80 \mathrm{~m} / \mathrm{s} / \mathrm{s}$.
When you have finished this, go to the website and check your answers. If you got a problem wrong, cross it off on the front, and do it correctly on the back.
1-3: A ball is launched at $27.2 \mathrm{~m} / \mathrm{s}$ at an angle of $75.0^{\circ}$ above horizontal on a level field. 1 . What time is the ball in the air?
2. What horizontal distance does it travel before hitting the ground again?
3. What is the greatest height the ball reaches? What is its speed at this height?
4. Use the range equation to find these ranges for the velocities and launch angles:

Velocity $=34.0 \mathrm{~m} / \mathrm{s}$, Launch Angle $=43.0^{\circ}$ Range $=$ $\qquad$

Velocity $=15.0 \mathrm{~m} / \mathrm{s}$, Launch Angle $=17.0^{\circ}$ Range $=$ $\qquad$
5. Use the range equation to find the proper launch angles for the following velocities and ranges:

Velocity $=34.0 \mathrm{~m} / \mathrm{s}$, Range $=100 . \mathrm{m}$, Launch Angles $=$ $\qquad$ and $\qquad$ degrees

Velocity $=12.0 \mathrm{~m} / \mathrm{s}$, Range $=5.00 \mathrm{~m}$, Launch Angles $=$ $\qquad$ and $\qquad$ degrees

## P3.3 Arc Practice Problems (Optional)

Round to the correct three figures, Ignore air friction and use the convention that down is negative. $\mathrm{g}=9.80 \mathrm{~m} / \mathrm{s} / \mathrm{s}$
 current of $0.820 \mathrm{~m} / \mathrm{s}$
a. What time will it take to cross the river?
b. How far downstream will the boat be carried in crossing the river?
c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity and label and calculate the angle it makes downstream, and the magnitude of the velocity.

2. A boat pointed straight across a 257 m wide river crosses it in 54.0 s . The river has a current of $0.460 \mathrm{~m} / \mathrm{s}$.
a. What is the speed of the boat with respect to the water?
b. How far downstream will the boat be carried in crossing the river?
c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity and label and calculate the angle it makes downstream, and the magnitude of the velocity.

3. A boat points straight across a river that is 142 m wide, with a current of $1.20 \mathrm{~m} / \mathrm{s}$. It lands 45.0 m downstream of where it started.
a. What time will it take to cross the river?
b. What is the speed of the boat with respect to the water?
c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity and label and calculate the angle it makes downstream, and the magnitude of the velocity.

4. A boat pointed straight across a 116 m wide river crosses in 67.0 seconds. In crossing it is carried 82.0 m downstream.
a. What is the speed of the boat with respect to the water?
b. What is the speed of the current?
c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity and label and calculate the angle it makes downstream, and the magnitude of the velocity.

[^0]Name $\qquad$

College you would like to go to $\qquad$
Show your work and circle your answers to receive full credit.
When you have finished this, go to the website and check your answers. If you got a problem wrong, cross it off on the front, and do it correctly on the back.

# 1-3: A boat points straight across a $\mathbf{6 8 . 0} \mathbf{m}$ wide river and crosses it in $\mathbf{1 8 . 2}$ seconds. In doing this it is carried downstream 23.7 m 

1. What the boat's velocity with respect to the water?
2. What is the speed of the current?
3. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity.

4-5: A boat pointed straight across has a velocity of $3.72 \mathrm{~m} / \mathrm{s}$ in a river with a current of $1.31 \mathrm{~m} / \mathrm{s}$. The river is 47.2 m wide.
4. What time will it take you to cross?
5. How far downstream is the boat carried as it crosses the river?

## P3.4 Boat Crossing River Problems (Optional)

| $\begin{array}{\|l\|} \hline 149 \mathrm{~s} \\ 122 \mathrm{~m} \\ 3.59 \mathrm{~m} / \mathrm{s} 13.2^{\circ} \mathrm{DS} \\ 4.76 \mathrm{~m} / \mathrm{s} \\ 24.8 \mathrm{~m} \end{array}$ | 1. a-c: A boat with a velocity in still water of $3.50 \mathrm{~m} / \mathrm{s}$ points straight across a 520 . m wide river with a current of $0.820 \mathrm{~m} / \mathrm{s}$ <br> a. What time will it take to cross the river? <br> b. How far downstream will the boat be carried in crossing the river? <br> c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity. <br> d-e: A boat pointed straight across a 257 m wide river crosses it in $\mathbf{5 4 . 0} \mathrm{s}$. The river has a current of $\mathbf{0 . 4 6 0 ~ m} / \mathrm{s}$. <br> d. What is the speed of the boat with respect to the water? <br> e. How far downstream will the boat be carried in crossing the river? |
| :---: | :---: |
| 66.0 s 87.2 m $2.52 \mathrm{~m} / \mathrm{s}, 31.5^{\circ} \mathrm{DS}$ $2.57 \mathrm{~m} / \mathrm{s}$ $0.533 \mathrm{~m} / \mathrm{s}$ | 2. a-c: A boat that can go $2.15 \mathrm{~m} / \mathrm{s}$ points straight across a 142.0 m wide river with a current of $1.32 \mathrm{~m} / \mathrm{s}$ <br> a. What time will it take to cross? <br> b. How far downstream will the boat be carried in this time? <br> c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity. <br> d-e: A boat takes 43.5 s to cross a river when it points straight across. The river is $\mathbf{1 1 2} \mathbf{~ m}$ wide, and the boat is carried downstream 23.2 m in crossing. <br> d. What is the speed of the boat with respect to the water? <br> e. What is the speed of the current? |
| $\begin{aligned} & \hline 67.1 \mathrm{~s} \\ & 194 \mathrm{~m} \\ & 3.10 \mathrm{~m} / \mathrm{s} 21.2^{\circ} \mathrm{DS} \\ & 391 \mathrm{~m} \\ & 104 \mathrm{~m} \end{aligned}$ | 3. a-c: A boat with a velocity (in still water) of $2.89 \mathrm{~m} / \mathrm{s}$ points straight across river with a <br>  <br> a. What time does it take to cross? <br> b. How wide is the river? <br> c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity. <br> d-e: A boat has a velocity of $5.43 \mathrm{~m} / \mathrm{s}$ (in still water) is pointed straight across a river with a <br>  <br> d. How wide is the river? <br> e. How far downstream will the boat be carried in crossing the river? |
| $\begin{array}{\|l\|} \hline 19.7 \mathrm{~s} \\ 1.21 \mathrm{~m} / \mathrm{s} \\ 4.67 \mathrm{~m} / \mathrm{s}, 15.0^{\circ} \mathrm{DS} \\ 2.92 \mathrm{~m} / \mathrm{s} \\ 0.901 \mathrm{~m} / \mathrm{s} \end{array}$ | 4. a-c: A boat with a speed of $4.51 \mathrm{~m} / \mathrm{s}$ points straight across a 89.0 m wide river and is carried downstream 23.8 m in crossing. <br> a. What time does it take to cross the river? <br> b. What is the speed of the current? <br> c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity. <br> d-e: A boat takes 87.0 s to cross a river when it points straight across. The river is $\mathbf{2 5 4} \mathbf{~ m}$ wide, and the boat is carried downstream 78.4 m in crossing. <br> d. What is the speed of the boat with respect to the water? <br> e. What is the speed of the current? |
| $\begin{array}{\|l\|} \hline 52.7 \mathrm{~s} \\ 2.81 \mathrm{~m} / \mathrm{s} \\ 3.07 \mathrm{~m} / \mathrm{s}, 23.8^{\circ} \mathrm{DS} \\ 287 \mathrm{~m} \\ 1.68 \mathrm{~m} / \mathrm{s} \end{array}$ | 5. a-c: A boat points straight across a 148 m wide river with a current of $1.24 \mathrm{~m} / \mathrm{s}$. In crossing <br>  <br> a. What time did it take to cross? <br> b. What is the speed of the boat with respect to the water? <br> c. What is the velocity (in angle magnitude notation) of the boat as it moves across the river? Draw a picture of the velocity. <br> d-e: A boat pointed straight across has a velocity of $5.21 \mathrm{~m} / \mathrm{s}$ with respect to the water, and crosses in $\mathbf{5 5 . 0} \mathbf{~ s . ~ I n ~ c r o s s i n g ~ t h e ~ b o a t ~ i s ~ c a r r i e d ~ d o w n s t r e a m ~ a ~ d i s t a n c e ~ o f ~} \mathbf{9 2 . 4} \mathbf{~ m}$. <br> d. How wide is the river? <br> e. What is the speed of the current? |

You will need a marble, a ruler ramp, a cup, 3 meter sticks, and a stopwatch.

## Part 1 - Determining the horizontal speed of the marble:

1. Set up a ramp on a table exactly 1 meter from the edge of the table, using two meter sticks as a guide. The marble should be able to roll down the ramp, across exactly one meter of table, and off the edge of the table presumably striking the floor some distance from the edge of the table. The ramp should be around 5 cm high on one end, so prop it up on a notebook or something not too high. (See my setup for reference)
2. Pick a unique distance (each partner should choose their own unique distance) up the ramp, and release it from rest 3 times from this position, timing the marble for the time it takes it to go 1.00 m

Times: $\qquad$
$\qquad$ Average $\qquad$

Velocity: $\qquad$

## Part 2 - Predicting where the marble will land on the floor:



Fill in the a $\mathrm{H} \mid \mathrm{V}$ table below:

1. Measure the height of the table in meters. This is your vertical displacement (X). Be careful to make it negative. On the "V" side you also know the initial velocity and acceleration.
2. Make the Vi and Vf on the "H" side your velocity from part 1
3. Solve for the X on the " H " side of your table. Show your calculations on the sides.


## Part 3 - Testing your prediction:

Put the target cup at that distance from the edge of the table (IQ on the line!), release from your unique position, and see if it goes in the cup. If this happens, you are obliged by long tradition to say "Eureka" loudly enough to be heard across the room.


[^0]:    a) $1.73 \mathrm{~m} / \mathrm{s}$, b) 1.22, c) $2.12 \mathrm{~m} / \mathrm{s}$ at $35.3^{\circ}$ downstream of straight across

