

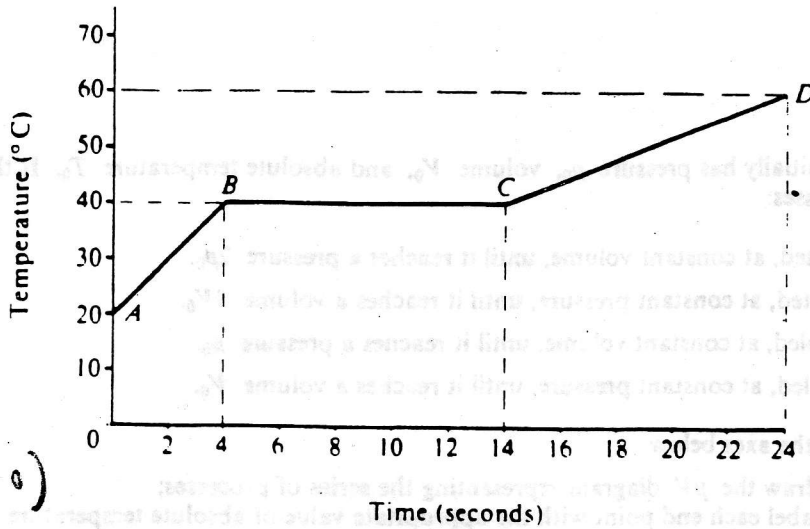
AP

Thermal

Questions.

Do these on  
this Paper.

(unless you really  
don't want to)



#1

A 0.020-kilogram sample of a material is initially a solid at a temperature of 20°C. Heat is added to the sample at a constant rate of 100 joules per second until the temperature increases to 60°C. The graph above represents the temperature of the sample as a function of time.

$1000 \text{ J/kg}^\circ\text{C}$   
 $5 \times 10^4 \text{ J/kg}$

- (a) Calculate the specific heat of the solid sample in units of joules per kilogram °C.
- (b) Calculate the latent heat of fusion of the sample at its melting point in units of joules per kilogram.
- (c) Referring to the three intervals AB, BC, and CD shown on the graph, select the interval or intervals on the graph during which:
  - i. the average kinetic energy of the molecules of the sample is increasing
  - ii. the entropy of the sample is increasing

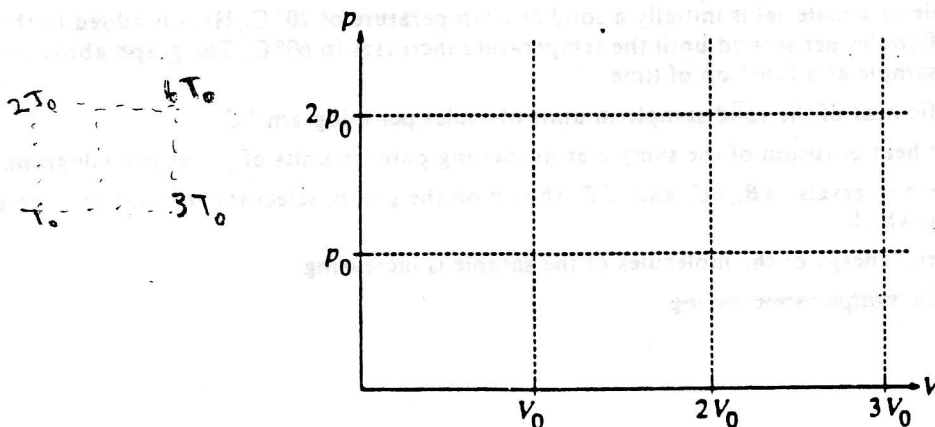
AB CD  
AB BC CD

#2 An ideal gas initially has pressure  $p_0$ , volume  $V_0$ , and absolute temperature  $T_0$ . It then undergoes the following series of processes:

- I. It is heated, at constant volume, until it reaches a pressure  $2p_0$ .
- II. It is heated, at constant pressure, until it reaches a volume  $3V_0$ .
- III. It is cooled, at constant volume, until it reaches a pressure  $p_0$ .
- IV. It is cooled, at constant pressure, until it reaches a volume  $V_0$ .

(a) On the axes below

- i. draw the  $pV$  diagram representing the series of processes;
- ii. label each end point with the appropriate value of absolute temperature in terms of  $T_0$ .



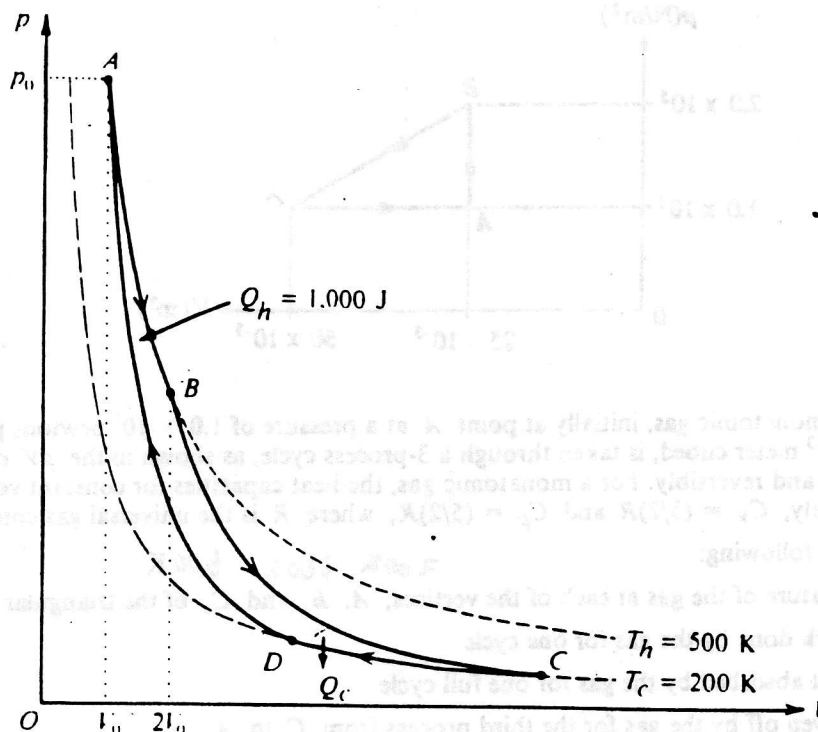
(b) For this series of processes, determine the following in terms of  $p_0$  and  $V_0$ .

- i. The net work done by the gas  $\rightarrow 2p_0V_0$
- ii. The net change in internal energy  $\rightarrow 0$
- iii. The net heat absorbed  $\rightarrow 2p_0V_0$

Optional (c) Given that  $C_p = \frac{5}{2}R$  and  $C_v = \frac{3}{2}R$ , determine the heat transferred during process 2 in terms of  $p_0$  and  $V_0$ .

$$\Delta Q = nC_p\Delta T = n\frac{5}{2}R(4T_0) = 10nRT_0 = 10p_0V_0$$

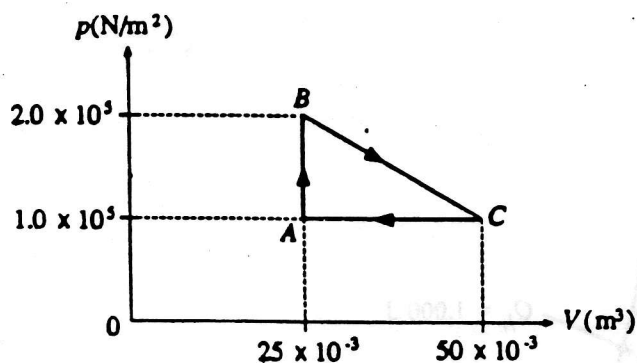
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# 3 • The  $pV$ -diagram above represents the states of an ideal gas during one cycle of operation of a reversible heat engine. The cycle consists of the following four processes.

Process	Nature of Process
AB	Constant temperature ( $T_h = 500$ K)
BC	Adiabatic
CD	Constant temperature ( $T_c = 200$ K)
DA	Adiabatic

- $p_B = p_0/2$  During process  $AB$ , the volume of the gas increases from  $V_0$  to  $2V_0$  and the gas absorbs 1,000 joules of heat.
- 1000 J (a) The pressure at  $A$  is  $p_0$ . Determine the pressure at  $B$ .
- increase (b) Using the first law of thermodynamics, determine the work performed by or on the gas during the process  $AB$ .
- 400 J (c) During the process  $AB$ , does the entropy of the gas increase, decrease, or remain unchanged? Justify your answer. *Optional*
- + work (d) Calculate the heat  $Q_c$  given off by the gas in the process  $CD$ .
- (e) During the full cycle  $ABCD$ , is the total work the gas performs on its surroundings positive, negative, or zero? Justify your answer.



# 4. One mole of an ideal monatomic gas, initially at point  $A$  at a pressure of  $1.0 \times 10^5$  newtons per meter squared and a volume of  $25 \times 10^{-3}$  meter cubed, is taken through a 3-process cycle, as shown in the  $pV$  diagram above. Each process is done slowly and reversibly. For a monatomic gas, the heat capacities for constant volume and constant pressure are, respectively,  $C_V = (3/2)R$  and  $C_P = (5/2)R$ , where  $R$  is the universal gas constant,  $8.32 \text{ J/mole} \cdot \text{K}$ .

Determine each of the following:

300K 600K 600K

1250J  
1250J  
6240J  
.17

- (a) the temperature of the gas at each of the vertices,  $A$ ,  $B$ , and  $C$ , of the triangular cycle
- (b) the net work done by the gas for one cycle
- (c) the net heat absorbed by the gas for one full cycle
- (d) the heat given off by the gas for the third process from  $C$  to  $A$
- (e) the efficiency of the cycle

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# 5. A freezer contains 20 kilograms of food with a specific heat of  $2 \times 10^3 \frac{\text{J}}{\text{kg} \cdot \text{C}}$ . The temperature inside the freezer is initially  $-5^\circ \text{C}$ . The freezer motor then operates for 10 minutes, reducing the temperature to  $-8^\circ \text{C}$ .

$1.2 \times 10^5 \text{ J}$  (a) How much heat is removed from the food during this time?

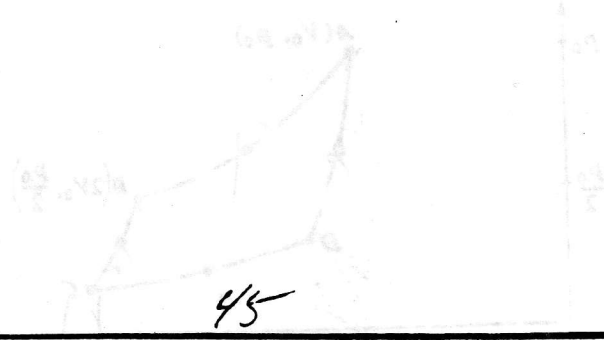
The freezer motor operates at 400 watts.

$2.4 \times 10^5 \text{ J}$  (b) How much energy is delivered to the freezer motor during the 10-minute period?

$3.6 \times 10^5 \text{ J}$  (c) During this time, how much total heat is ejected into the room in which the freezer is located?

$6.4^\circ \text{C}$  (d) Determine the temperature change in the room if the specific heat of air is  $700 \frac{\text{J}}{\text{kg} \cdot \text{C}}$ . Assume there are 80 kilograms of air in the room, the volume of the air is constant, and there is no heat loss from the room.

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(10) In the table below, for each part of the cycle indicate with a plus (+) or minus (-) whether the heat is added to or removed from the gas. If the temperature change  $\Delta T$  is positive, negative, or zero, indicate that with a plus (+), minus (-), or zero (0). If the heat added to the gas, and  $\Delta T$  is positive when the temperature of the gas increases.

Part of Cycle	Heat Added (+ or -)	Temperature Change $\Delta T$ (+, -, or 0)
AB		
BC		
CD		
DA		

+  
-  
0  
0  
+

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# 6

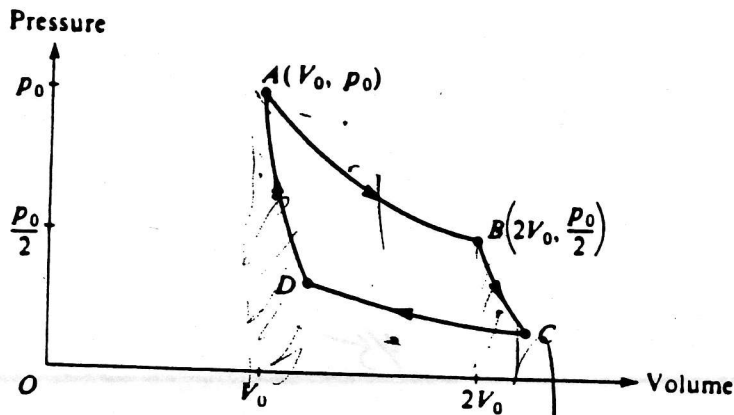
A proposed ocean power plant will utilize the temperature difference between surface seawater and seawater at a depth of 100 meters. Assume the surface temperature is  $25^\circ$  Celsius and the temperature at the 100-meter depth is  $3^\circ$  Celsius.

0.74 (a) What is the ideal (Carnot) efficiency of the plant?

1250 MW (b) If the plant generates useful energy at the rate of 100 megawatts while operating with the efficiency found in part (a), at what rate is heat given off to the surroundings?

$2.77 \times 10^{-9}$  kg/s (c) A nuclear power plant operates with an overall efficiency of 40 percent. At what rate must mass be converted into energy to give the same 100-megawatt output as the ocean power plant above? Express your answer in kilograms per second.

The diagram below represents the Carnot cycle for a simple reversible (Carnot) engine in which a fixed amount of gas, originally at pressure  $p_0$  and volume  $V_0$ , follows the path ABCDA.



(d) In the chart below, for each part of the cycle indicate with +, -, or 0 whether the heat transferred  $Q$  and temperature change  $\Delta T$  are positive, negative, or zero, respectively. ( $Q$  is positive when heat is added to the gas, and  $\Delta T$  is positive when the temperature of the gas increases.)

+ 0  
0 -  
- 0  
0 +

	$Q$	$\Delta T$
AB		
BC		
CD		
DA		

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