

Angular Kinematics problems from 8.1

Tangential Relationships: $s = \theta r$, $v = \omega r$, $a = \alpha r$

1. A 0.0760 m diameter (76 mm) skateboard wheel rolls through 137 rotations. What linear distance did it travel? (32.7 m)
2. What is the angular acceleration of a 0.630 m diameter bicycle wheel if it is accelerating linearly at 8.20 m/s/s? (26.0 rad/s/s)
3. A 0.0660 m diameter skateboard wheel travels 12.0 m. How many rotations does it go through? (57.9 rotations)
4. A 0.650 m diameter wheel accelerates at 1.54 rad/s/s. What is the tangential acceleration of the edge? (0.5005 m/s/s)
5. A wheel goes through 143 rotations when it rolls linearly 14.2 m. What is the radius of the wheel? (0.0158 m)

Tangential Relationships with unit conversions: **1 rev or rot = 2π radians, 1 minute = 60 seconds**

6. What is the linear velocity 0.120 m from the center of a grinding disk spinning at 1450 RPM? (18.2 m/s)
7. What is the angular velocity of a 0.920 m radius aircraft tire in rotations/second when it has a linear velocity of 48.0 m/s? (8.30 rot/s)
8. A merry go round spins at 0.590 rotations/second. What is the tangential velocity 1.80 m from the center? (6.67 m/s)
9. A 0.940 m diameter wheel has a tangential velocity at its edge of 25.0 m/s. What is its angular velocity in RPM? (508 RPM)
10. A hard drive spins at 7200 RPM. What distance from the center has a tangential velocity of 12.0 m/s? (0.0159 m)

Simple Rotational kinematics: $v = u + at$, $s = (u+v)t/2$, $v^2 = u^2 + 2as$, $s = ut + \frac{1}{2}at^2$

11. A drill going 98.0 rad/s decelerates at -1.20 rad/s/s for 15.0 s. What is the final angular velocity in rad/s? (80.0 rad/s)
12. A drill speeds up from rest to 156 rad/s in 5.70 s. Through what angle in radians does it go? (445 rad)
13. A drill goes through 132 radians in 8.80 s slowing to rest. What was its initial angular velocity in rad/s? (30.0 rad/s)
14. A drill speeds up from 11.0 rad/s to 35.0 rad/s in 184 radians. What is its angular acceleration? (3.00 rad/s/s)
15. A drill goes through 526 radians accelerating at 2.58 rad/s/s from rest. What is its final angular velocity in rad/s? (52.1 rad/s)

Rotational Kinematics with unit conversions:

16. A motor speeds up from 1350. RPM with an angular acceleration of 2.90 rad/s/s for 19.0 seconds. Through what angle in radians does it rotate? (3210 rad)
17. A car tire initially rotating at 37.0 rotations per second slows down through 148 rotations in 5.20 seconds. What is its final angular velocity in rotations per second? (19.9 rot/s)
18. A drill speeds up from 680. RPM to 1540 RPM with an acceleration of 1.80 rad/s/s. How many rotations does it go through? (926 rotations)
19. A skateboard wheel speeds up from 5.30 rotations/sec to 12.0 rotations/s in 9.00 seconds. What is the angular acceleration in rad/s/s? (4.68 rad/s/s)
20. A turntable accelerates at 0.835 rad/s/s from rest to 33.3 RPM. What is its angular displacement in radians? (7.28 rad)

Rotational Kinematics with tangential relationships:

21. A car with 0.340 m radius tires going 19.2 m/s decelerates at 1.20 m/s/s for 2.30 s. What is the final angular velocity of the tires? (48.4 rad/s)
22. A car with 0.840 m diameter wheels accelerates from rest with an acceleration of 6.40 m/s/s for 3.50 seconds. Through what angle in radians do the wheels go? (93.3 radians)
23. A 0.110 m radius ball going 5.80 m/s rolls to a stop in 9.70 seconds. What was the angular acceleration of the ball in rad/s/s? (-5.44 rad/s/s)
24. A 0.360 m radius car tire goes from 12.5 rad/s to 36.8 rad/s with a linear acceleration of 3.90 m/s/s. What linear distance does the car travel? (19.9 m)
25. A 0.125 m radius grinding wheel speeds up from 142 rad/s to 259 rad/s in 13.0 s. Through what distance does a point in the edge of the wheel travel in this time? (326 m)

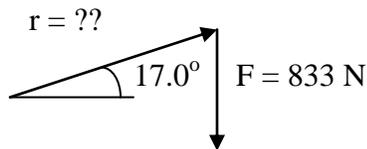
Name _____

Favorite Film Maker _____

Show your work, and circle your answers and use sig figs to receive full credit.

I (about centers): cylinder = $\frac{1}{2}mr^2$, ring/point = mr^2 , sphere = $\frac{2}{5}mr^2$, rod = $\frac{1}{12}mL^2$ (= $\frac{1}{3}mL^2$ about end)

1. A mechanic needs to exert 385 mN of torque. He weighs 833 N and he stands on the handle of his wrench that is making a 17.0° angle above the horizontal. How far from the center must he stand? (Be careful what you use for the angle)



2. What is the acceleration of a flywheel with a moment of inertia of 0.145 kg m^2 if a torque of 2.80 mN acts on it?

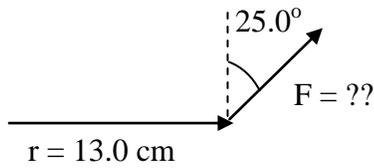
3. A 0.680 m diameter flywheel has a moment of inertia of 0.243 kg m^2 . What is the angular acceleration of the flywheel if you exert 4.50 N tangentially at the edge to speed it up?

4. A 0.210 m radius grinding disk is spinning at 1350 RPM . If it goes through 85.0 rotations being brought to rest by a 1.20 N frictional force applied tangentially at its edge, what is the moment of inertia of the disk?

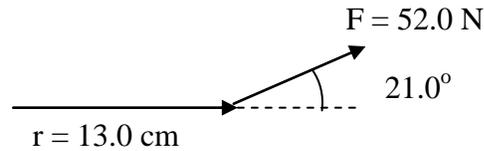
5. A 4.30 m diameter (cylindrical) merry go round going 45.0 RPM stops in 37.0 rotations because of an 8.30 N force applied tangentially at the edge. What is the mass of the merry go round?

Angular Dynamics problems from 8.2

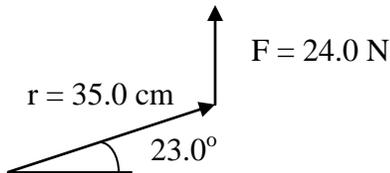
A. What force acting at 25.0° with a line perpendicular to the end of a 13.0 cm long wrench will generate 7.80 mN of torque about the left side of the wrench? (66.2 N)



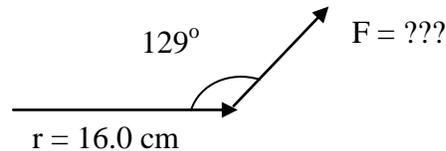
B. Calculate the torque about the left side of the wrench if 52.0 N acts at an 21.0° angle with the end of a 13.0 cm long wrench. (2.42 mN)



C. A 35.0 cm wrench makes a 23.0° angle above the horizontal. What is the torque about the left side of the wrench if a 24.0 N force is exerted vertically upward at the end? (7.73 mN)



D. A force is exerted at an angle of 129° with a 16.0 cm wrench as shown below. Calculate the force needed to create 3.80 mN of torque about the left side of the wrench. (30.6 N)



Moments of inertia: Cylinder: $I = \frac{1}{2} mr^2$, Sphere: $I = \frac{2}{5} mr^2$, Thin Ring or Point Mass: $I = mr^2$

Simple $F = ma$ problems: $\Gamma = I\alpha$

1. A baton requires 5.70 mN of torque to accelerate at 18.4 rad/s^2 about its center. What is the moment of inertia? (0.310 kgm^2)
2. A flywheel with a moment of inertia of 0.859 kg m^2 accelerates at 13.0 rad/s^2 . What is the torque? (11.2 mN)
3. A motor with 43.0 mN of torque accelerates at 153 rad/s^2 . What is its moment of inertia? (0.281 kgm^2)
4. A torque of 21.0 mN acts on a motor with a moment of inertia of 1.53 kg m^2 . What is the angular acceleration? (13.7 rad/s^2)
5. What torque will accelerate a motor with a moment of inertia of 3.87 kg m^2 at 6.60 rad/s^2 ? (25.5 mN)

$F = ma$ problems, but $I = \frac{1}{2} mr^2$ (cylinder), $\frac{2}{5} mr^2$ (sphere), or kinematics, or $\Gamma = rF$

6. A 0.400 m diameter, 4.30 kg sphere accelerates about its center at 6.80 rad/s^2 . What is the torque? (0.468 mN)
7. A drill with a moment of inertia of 0.0180 kg m^2 is slowed by a frictional torque of 0.270 mN. If it is moving at 142 rad/s , how many radians will it go through before it stops? (672 rad)
8. A grinding wheel with a diameter of 0.640 m and a moment of inertia of 0.172 kg m^2 decelerates at -8.90 rad/s^2 because of a tangential friction force applied at the edge. What is this force? (4.78 N)
9. A torque of 19.0 mN acts on a flywheel with a moment of inertia of 3.20 kg m^2 . If it starts at rest, in what time will it go through 16.0 radians? (2.32 s)
10. A torque of 3.50 mN acts on a 7.10 kg, 0.132 m diameter shot put. (a sphere) What is the angular acceleration of the sphere? (283 rad/s^2)

Same as above with unit conversions:

11. A 0.219 m diameter bowling ball has a tangential force 5.50 N acting on it and it accelerates from rest going through 13.0 rotations in 3.21 seconds. What is the moment of inertia of the ball? (0.0380 kgm^2)
12. A 0.310 m radius flywheel (essentially a thin ring) with a mass of 3.20 kg. What is its rate of deceleration if you exert a force of 2.20 N tangentially at its edge? (2.22 rad/s^2)
13. A flywheel is a 13.2 kg 1.80 m diameter thin ring. If you exert a force of 51.0 N tangentially at its edge, what is its angular acceleration? (4.29 rad/s^2)
14. A flywheel that is a 0.730 m diameter thin ring with a mass of 16.0 kg would require what torque to accelerate from rest to 1120 RPM in 8.10 seconds? (30.9 mN)
15. What is the moment of inertia of a 0.258 m radius flywheel if when you exert a tangential force of 11.5 N at the edge it accelerates from rest to 680. RPMs in 123 rotations? (0.904 kgm^2)

Same as above with unit conversions and kinematics:

16. A 161 kg 4.72 m diameter (cylindrical) merry go round is sped up from rest by a 25.0 N force applied tangentially at its edge. What is its speed in RPMs after 38.0 seconds? (47.8 RPM)
17. A 2.10 m radius, 351 kg (cylindrical) merry go round spinning at 75.0 RPM slows to a halt in 11.5 rotations. What force applied tangentially at the edge would cause this? (157 N)
18. A 232 kg 4.10 m diameter (cylindrical) Merry go round is stopped from a speed of 94.0 RPM in 55.0 seconds. What frictional force applied tangentially at the edge would cause this? (42.6 N)
19. A 243 kg 1.70 m radius (cylindrical) merry go round stops from a speed of 68.0 RPM because of a frictional force applied at the edge of 8.50 N. How many rotations does it go through in stopping? (98.1 rotations)
20. A 4.60 m diameter (cylindrical) merry go round speeds up from rest going through 5.10 rotations in 41.0 seconds because of a 15.0 N force applied tangentially at the edge. What is the mass of the merry go round? (342 kg)

Name _____

Favorite Musician _____

Show your work, and circle your answers and use sig figs to receive full credit.

I (about centers): cylinder = $\frac{1}{2}mr^2$, ring/point = mr^2 , sphere = $\frac{2}{5}mr^2$, rod = $\frac{1}{12}mL^2$ (= $\frac{1}{3}mL^2$ about end)

1-3: A 12.0 g, 0.0140 m radius marble rolls down an incline that is 3.80 m long, and loses 0.120 m of elevation.

1. Set up the appropriate dynamics or conservation of energy equation, substitute for ω or α , and for I, and solve for v or a. Show your steps below. Give an exact answer. $a = \frac{5}{7}g \cdot \sin(\theta)$ $v = \sqrt{\frac{10}{7}gh}$

2. Solve for the final velocity of the marble at the bottom of the incline.

3. Calculate the acceleration of the marble as it rolls down the incline.

4-5: A 45.0 kg child is 1.80 m from the center of a 2.00 m radius merry go round that is a 160. kg cylinder.

4. If the merry go round speeds up from 1.40 rad/s to 2.10 rad/s in 4.00 seconds, what torque was applied?

5. If the merry go round is spinning at 45.0 RPM and the child moves from 1.80 m from the center to 0.600 m from the center, what is the new angular velocity of the merry go round in RPMs?

Angular Energy and Momentum problems from 8.3

A Basic Energy:

1. What is the kinetic energy of a flywheel with a moment of inertia of 12.4 kgm^2 that is spinning at 17.8 rad/s ? (1960 J)
2. A flywheel spins at 87.0 rot/s when it is storing $12,500 \text{ J}$ of kinetic energy. What is its moment of inertia? (0.0837 kgm^2)
3. What is the speed in RPMs of a 4.50 kg 34.0 cm diameter cylindrical grinding disk if it has $340. \text{ J}$ of rotational kinetic energy? (977 RPM)
4. A 4.50 kg 12.0 cm radius bowling ball is rolling at 3.20 m/s . What is its translational kinetic energy? What is its rotational kinetic energy? What is its total kinetic energy? If it rolled from rest down a hill, how high is the hill? (23.0 J , 9.22 J , 32.3 J 0.731 m)
5. If linear work is given by $W = Fs$, then angular work is $W = I\theta$. Use energy to find the angular final velocity of a flywheel that has a moment of inertia of 8.50 kgm^2 after it has been sped from rest up by a torque of 52.0 mN through 84.0 radians. (32.1 Rad/s)

B Rolling problems:

For all of these:

- a. Set up the appropriate dynamics or conservation of energy equation, substitute for ω or α , and for I , and solve for v or a . Show your steps Give an exact answer. (you will need to give an answer with a simplified fraction!)
 - b. Solve for the final velocity of the marble at the bottom of the incline.
 - c. Calculate the acceleration of the marble as it rolls down the incline.
1. A 11.0 g , 0.0110 m radius unique circular solid with a moment of inertia given by $\frac{2}{3}mr^2$, rolls down an incline that is 2.60 m long, and loses 0.560 m of elevation. (2.80 m/s , 1.51 m/s/s)
 2. A 13.0 g , 0.0130 m radius unique circular solid with a moment of inertia given by $\frac{1}{2}mr^2$, rolls down an incline that is 5.10 m long, and loses 1.90 m of elevation. (4.99 m/s , 2.44 m/s/s)
 3. A 15.0 g , 0.0140 m radius unique circular solid with a moment of inertia given by $\frac{1}{3}mr^2$, rolls down an incline that is 4.10 m long, and loses 1.30 m of elevation. (4.37 m/s , 2.33 m/s/s)
 4. A 143.0 g , 0.0450 m radius unique circular solid with a moment of inertia given by $\frac{2}{7}mr^2$, rolls down an incline that is 3.30 m long, and loses 1.10 m of elevation. (4.10 m/s , 2.54 m/s/s)
 5. A 12.0 g , 0.0120 m radius unique circular solid with a moment of inertia given by $\frac{7}{8}mr^2$, rolls down an incline that is 3.20 m long, and loses 0.340 m of elevation. (1.89 m/s , 0.556 m/s/s)

C Basic Momentum:

1. What is the angular momentum of a disk with a moment of inertia of 0.145 kgm^2 that is spinning at 45.0 rad/s ? ($6.53 \text{ kgm}^2/\text{s}$)
2. What angular velocity in rad/s must a $120. \text{ kg}$ 1.80 m radius cylindrical merry go round go to have $2360 \text{ kg m}^2/\text{s}$ of angular momentum? (12.1 rad/s)
3. What torque would speed up a merry go round with 296 kgm^2 of rotational inertia from rest to 6.28 rad/s in 32.0 seconds? (58.1 mN)
4. A 2.60 kg cylindrical flywheel with a diameter of 54.0 cm is spinning at 115 rad/s . If a frictional torque of 1.30 mN acts on it, in what time would it stop? (8.38 s)
5. A ballerina spinning at 1.20 rev/sec with a moment of inertia of 2.60 Kg m^2 pulls her arms in so that her new moment of inertia is 1.80 Kg m^2 . What is her new angular speed? (1.73 rev/sec)
6. A group of children playing on a merry go round spinning at 52.0 rpm with a moment of inertia of $200. \text{ Kg m}^2$ move to its center so that the new angular velocity is 86.7 RPM . What is the new moment of inertia? ($120. \text{ kgm}^2$)

D Momentum Questions:

- 1. A 54.0 kg child is 1.80 m from the center of a 2.10 m radius merry go round that is a $170. \text{ kg}$ cylinder.**
 - a. If a torque of 92.0 mN is applied for 13.0 seconds, what is the change in angular velocity? b. The child moves out to a distance of 2.10 m , and as a result the merry go round is spinning at 0.450 rot/s . What was its initial angular velocity in rot/s ? (2.18 rad/s , 0.502 rot/s)
- 2. A 68.0 kg child is 2.70 m from the center of a 3.30 m radius merry go round that is a $140. \text{ kg}$ cylinder.**
 - a. For what time must a torque of 31.0 mN act to accelerate the merry go round from rest to 5.20 rad/s ? b. When the merry go round is spinning at 21.0 RPM , the child moves in to a distance of 1.90 m from the center. What is the final angular velocity in RPM ? (211 s , 26.2 RPM)
- 3. A 51.0 kg child is 1.10 m from the center of a 2.40 m radius merry go round that is a $160. \text{ kg}$ cylinder.**
 - a. If the merry go round speeds up from rest to 4.70 rad/s in 14.0 seconds, what torque was acting? b. When the merry go round is rotating at 0.970 rot/s , the child moves out to a distance of 2.30 m from the center. What is the new angular velocity of the merry go round in rot/s ? (175 mN , 0.694 rot/s)
- 4. A 41.0 kg child is 2.20 m from the center of a 2.40 m radius merry go round that is a $150. \text{ kg}$ cylinder.**
 - a. If a torque of 95.0 mN acts on the merry go round for 8.00 seconds, what is the change in angular velocity? b. The child moves in to a distance of 1.10 m from the center, and as a result, the angular velocity of the merry go round is 65.0 RPM . What was the initial angular velocity in RPM ? (1.21 rad/s , 49.7 RPM)
- 5. A 58.0 kg child is 1.00 m from the center of a 2.20 m radius merry go round that is a $180. \text{ kg}$ cylinder.**
 - a. For what time must a torque of 35.0 mN act on the merry go round to change its angular velocity from rest to 3.50 rad/s ? b. If the merry go round is spinning at 0.780 rot/s , and the child moves out to 2.20 m from the center, what is the final angular velocity in rot/s ? (49.4 s , 0.537 rot/s)

So you think you're so dang smart?

Giancoli #67: Suppose a 55-kg person stands at the edge of a 6.5-m diameter merry-go-round turntable that is mounted on frictionless bearings and has a moment of inertia of 1700 kgm^2 . The turntable is at rest initially, but when the person begins running at a speed of 3.8 m/s (with respect to the turntable) around its edge, the turntable begins to rotate in the opposite direction. Calculate the angular velocity of the turntable.
(-0.30 rad/s)

Gyroscope Investigation

1. You will need a gyroscope, a gear puller, a gyroscope stand, and a love for rotational mechanics.
2. Get the gyroscope spinning by using the gear puller. Hold the gyroscope firmly, and pull the handle - being careful not to strip the little teeth. Play with it over a table. If it drops on the floor it will break. Come up with a stupid gyroscope trick.
3. Get the gyroscope spinning anti-clockwise as seen from above (This way the L vector is pointing up), put the bottom of the gyro into stand. Note carefully which way the gyroscope precesses.
4. **Draw careful diagrams** that a) show the direction of the torque on the gyroscope (Due to gravity) the axis about which this torque acts is the stand $\Gamma = r \times F$, so r is away from the stand, F is straight down, b) show the direction of the angular momentum vector, c) show that the direction of precession has the tip of the L vector going in the direction of the torque.
5. Answer these questions:
 - A. Measure the mass of the rotor by weighing the gyroscope, and subtracting the 23.5 grams that is the cage. Measure the radius of the rotor, and use a formula like $I = mr^2$ (or is it $.9mr^2$? - feel free to make your own formula) to **find the moment of inertia of the rotor in kgm^2** .
 - B. The axle has a diameter of 3.9 mm (0.0039 m). Supposing the puller was moving about 1.5 m/s at the end of your pull,
 1. **calculate the angular velocity of the gyro**, (use $v = \omega r$) and
 2. **calculate the angular momentum of the gyro**. ($L = I\omega$)
 - C. Calculate the **angular momentum of the earth** ($L = I\omega$). (use the interwebs to find the mass, radius, and period of rotation. Assume the earth is a sphere ($\frac{2}{5}mr^2$). $\omega = 2\pi/T$. You can also just go to wolfram alpha and type "angular velocity of the earth") Show that it is about $7 \times 10^{33} \text{ kgm}^2/\text{s}$ (be a bit more exact)
6. Leave your gyroscope exactly the way you found it.

Here's what you turn in:

1. The diagram as explained in part 4.
2. The answers for part 5.

